

①

1) $A = \text{סרבת הניסוי}$
 $B = \text{סרבת ה"ש}$
 $C = \text{סרבת תחילת}$

	A	$\bar{A}$	
B	0.2	0.4	0.6
$\bar{B}$	0.3	0.1	0.4
	0.5	0.5	

1c) $P(A) = \boxed{0.5}$ 2) $P(\bar{A} \cap B) = \boxed{0.4}$

3) $P(\bar{B} | C) = \frac{P(\bar{B} \cap C)}{P(C)} = \frac{P(\bar{B} \cap A)}{P(C)}$
 $= \frac{0.3}{0.7} = \boxed{\frac{3}{7}}$

2) a) $\frac{\binom{7}{4} \binom{8}{2} + \binom{7}{5} \binom{8}{1} + \binom{7}{6}}{\binom{15}{6}}$

$= \boxed{\frac{3}{13} = 0.23}$

2) $A = \text{פרט 3 ימים}$

$B = \text{תחילת הניסוי}$

$P(B) = 1 - \frac{\binom{8}{6}}{\binom{15}{6}} = 0.994$

$$P(A \cap B) = \frac{\binom{7}{3} \binom{8}{3}}{\binom{15}{6}} = 0.391$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{0.391}{0.994} = \boxed{0.394}$$

$$3) X \sim N(76, \sigma)$$

$$P(X < 60) = 0.1, \quad P(Z < \frac{60-76}{\sigma}) = 0.1$$

$$1 - \Phi\left(\frac{16}{\sigma}\right) = 0.1, \quad \Phi\left(\frac{16}{\sigma}\right) = 0.9$$

$$\frac{16}{\sigma} = 1.28, \quad \sigma = 12.5$$

$$c) P(X > 90) = P(Z > \frac{90-76}{12.5})$$

$$= 1 - \Phi(1.12) = 1 - 0.8686 = \boxed{0.1314}$$

$$2) P(X < K) = 0.05, \quad P(Z < \frac{K-76}{12.5}) = 0.05$$

$$\Phi\left(\frac{K-76}{12.5}\right), \quad \frac{K-76}{12.5} = -1.645$$

$$\boxed{K = 55.44}$$

$$4) c) \left(\frac{4}{2}\right) \left(\frac{1}{6}\right)^2 \left(\frac{5}{6}\right)^2 = \boxed{0.1116}$$

A = תוצאות 6 ניסויים

B = תוצאות 3 ניסויים

③

$$P(B) = \binom{4}{3} \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right) = \frac{1}{4}$$

$$P(A \cap B) = \frac{4 \cdot \binom{3}{2} \cdot 2^2 \cdot 3}{6^4} = \frac{1}{9}$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{\frac{1}{9}}{\frac{1}{4}} = \boxed{\frac{4}{9}}$$

$$E) \frac{6 \cdot 5 \cdot 4 \cdot 3}{6^4} = \boxed{\frac{5}{18} = 0.25}$$

$$3) \frac{\binom{6}{2} \cdot \binom{4}{2}}{6^4} = \boxed{\frac{5}{72} = 0.069}$$

$$5) X \sim B(3, \frac{1}{3})$$

$$E(X) = n \cdot p = 3 \left(\frac{1}{3}\right) = \boxed{1}$$

$$\text{Var}(X) = n \cdot p \cdot q = 3 \left(\frac{1}{3}\right) \left(\frac{2}{3}\right) = \boxed{\frac{2}{3}}$$

1 1 8 5 3 1 1 1 8 2 0 2 7 7 i 1 c

X	P(X)
0	8/27
1	12/27
2	6/27
3	1/27

(4)

$$X \sim G\left(\frac{1}{6}\right)$$

$$6) \quad 1c) \quad P(X < 8) = 1 - P(X \geq 8) = 1 - \left(\frac{5}{6}\right)^7$$

$$= \boxed{0.72}$$

$$\begin{aligned} 2) \quad & P(X=2) + P(X=4) + P(X=6) + \dots \\ &= \left(\frac{5}{6}\right) \cdot \frac{1}{6} + \left(\frac{5}{6}\right)^3 \left(\frac{1}{6}\right) + \left(\frac{5}{6}\right)^5 \frac{1}{6} + \dots \\ &= \frac{5}{36} \left(1 + \left(\frac{5}{6}\right)^2 + \left(\frac{5}{6}\right)^4 + \dots\right) \\ &= \frac{5}{36} \cdot \left(\frac{1}{1 - \left(\frac{5}{6}\right)^2}\right) = \frac{5}{36} \cdot \left(\frac{36}{36 - 25}\right) \\ &= \boxed{\frac{5}{11}} = 0.45 \end{aligned}$$

$$c) \quad A = \text{სიღრმე 6-მ ნიადა}$$

$$B = \text{სიღრმე 8-ის ზღონ}$$

$$P(B) = \frac{5}{11}, \quad P(A \cap B) = P(X=2) + P(X=4)$$

$$= \frac{5}{6} \cdot \frac{1}{6} + \left(\frac{5}{6}\right)^3 \left(\frac{1}{6}\right) = 0.235$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{0.235}{0.45} = \boxed{0.52}$$

(5)

$$2) P(A) = 1 - P(X \geq 4) = 1 - \left(\frac{5}{6}\right)^3 = 0.421 = \frac{91}{216}$$

$$P(B) = \frac{6}{11} = 0.54$$

$$P(A \cap B) = P(X=1) + P(X=3)$$

$$= \frac{1}{6} + \left(\frac{5}{6}\right)^2 \left(\frac{1}{6}\right) = \frac{61}{216}$$

$$P(A \cap B) = \frac{61}{216}, \quad P(A) \cdot P(B) = \left(\frac{91}{216}\right) \cdot \left(\frac{6}{11}\right) = \frac{91}{396}$$

$$P(A \cap B) \neq P(A) \cdot P(B) \Rightarrow \boxed{P \text{ " 18n"}}$$